

Creating Code writing algorithms for producing n -lagged variables

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ABSTRACT

As a predictive modeler with time-series data there is a continuous search for new and “better” techniques to produce more precise forecasts. One of these techniques is to include lagged values as predictors in a model which leads to a technical coding question. How does one produce an n -number (large number of) of lagged variables without having to type every single lagged instance?

INTRODUCTION

How can a series of 360 (or more) lagged columns be created in a data set without writing every single lag statement? If one has SAS/ETS then the solution may be easier but may still be prone to typing errors and retain a level of mind-numbing inhibition as one types: 1 2 3 4180.... etc. If SAS/ETS is not available then such columns can be added within a data step using the `lag()` function- but will require ever more mind numbing coding to produce 360+ lagged variable increasing the probability of syntax errors- and proofing becomes even more challenging. The proposed solution we demonstrate is similar in either case and can be leveraged in a similar way for other problems requiring a large number of iterative columns of transformations.

The data presented is based on the neural network forecasting competition of 2008 using altered ATM forecast volumes per day. This is a common scenario for banks to be able to forecast either the amount of withdrawals (total cash taken out) so that it may be know when or how often to service an ATM. The variable of to be forecasted using the lags in these examples is called “usage” which is a transformation of Withdrawals for the ATMs.

ADDING N-LAGGED COLUMNS USING SAS/ETS (assuming no missing data)

The proc panel procedure is very useful for producing lagged columns with syntax like:

```
PROC PANEL DATA=TRAIN;
  ID ATM TRANDATE;
  LAG USAGE (1 2 3) /OUT=IMPUTED_LAG;
RUN;
```

However if 360 lagged columns are desired all values 1- 360 would have to entered like:

```
PROC PANEL DATA=TRAIN;
  ID ATM TRANDATE;
  LAG USAGE (1 2 3...180...360) /OUT=IMPUTED_LAG;
RUN;
```

The solution which is similar in nature for the non ETS method to be discussed is 3 steps:

- 1) Produce a data set of all values

```
DATA X;
  DO X=1 TO 360;
    OUTPUT;
  END;
RUN;
```

- 2) Create a global variable using the “separated” feature in proc sql of the entire data set

```
PROC SQL NOPRINT;
  SELECT X INTO:LG SEPARATED BY ' ' FROM X ;
QUIT;
```

- 3) Insert the global variable into the proc panel procedure.

```
PROC PANEL DATA=TRAIN;
    ID ATM TRANDATE;
    LAG USAGE (&LG.) /OUT=IMPUTED_LAG;
RUN;
```

Adding N-lagged columns without using SAS/ETS(assuming no missing data)

Lagged variables within a data step can be very easily achieved in a data step if the data is sorted correctly and the data step contains syntax like:

```
lag1=lag1(usage);
lag2=lag2(usage);
.
.
.
lag<n>=lag<n>(usage);
```

This process adds n-lagged variables to the data step. A word of caution however- if the data is meant to be used with by processing, such as this example with multiple ATMs, then care needs to be taken so that the lag value of one entity (ATM) does not carry over to another entity (ATM). The solution for this scenario is to:

- 1) Create two temporary lag columns- one for the value the other for the entity (ATM)
- 2) Only create a lag value if the lag of the entity (ATM) matches the current record entity (ATM).

```
DATA LAG_NO_ETS;
    SET TRAIN;
    BY ATM;
    TMP_LAG1=LAG1 (USAGE) ;
    TMP_LAG2=LAG2 (USAGE) ;
    TMP_LAG3=LAG3 (USAGE) ;

    ATM_LAG1=LAG1 (ATM) ;
    ATM_LAG2=LAG2 (ATM) ;
    ATM_LAG3=LAG3 (ATM) ;

    IF ATM=ATM_LAG1 THEN LAG1=TMP_LAG1;
    IF ATM=ATM_LAG2 THEN LAG2=TMP_LAG2;
    IF ATM=ATM_LAG3 THEN LAG3=TMP_LAG3;
    DROP TMP_LAG1--ATM_LAG3;
RUN;
```

At this point it may be clear that creating 360+ lagged variables would require a significant amount of coding as 3 separate lines are needed for each lag.

As demonstrated in the SAS/ETS example above the strategy of creating a data set of the actual line code and then using global variables to call appears to be a logical solution- but as shown below this solution is not sufficient without extra modification:

Function style macro:

```
*Function Style Macro;
%MACRO L (J) ;
L&J.=LAG&J. (USG_IMP) ;
ATM_LAG&J.=LAG&J. (ATM) ;
IF ATM=ATM_LAG&J. THEN LAG&J.=TMP_LAG&J.;
%MEND;
```

```

**Failed attempt to create 360 lagged values using the function style macro;
DATA LAG_NO_ETS;
    SET TRAIN;
    BY ATM;
    DO I=1 TO 360;
        %L(I)
    END;
    DROP I;
RUN;

```

Resulting in the following error message:

```

Log - (Untitled)
12 DATA LAG_NO_ETS;
13 SET TRAIN;
14 BY ATM;
15 DO I=1 TO 360;
16 %L(I)
NOTE: Line generated by the macro variable "J".
1 LAGI
-----
68
NOTE: Line generated by the macro variable "J".
1 LAGI
-----
68
ERROR 68-185: The function LAGI is unknown, or cannot be accessed.

17 END;
18 DROP I;
19 RUN;

```

Figure 1. Log of Failed Attempt

This problem results from the fact that the macro is written prior to processing the data step and "J" resolves to "I" rather than what "I" resolves to. The alternative to work around this issue is to imitate what was presented for the SAS/ETS solution presented with the following steps:

- 1) Create a syntax data set with a do loop that produce the SAS code desired to be processed (including the semicolons)
- 2) Create macro variables that resolve to the statements in the syntax data set
- 3) Insert the macro variable to resolve within the data step

```

*STEP 1) CREATING SYNTAX DATA SET;
%LET LAGS=360;

DATA TMP (DROP=I);
    FORMAT TMP_LAG ATMLAG LAG $100.;
    DO I=1 TO &LAGS.;
        TMP_LAG=COMPRESS("TMP_LAG"||I||"=LAG"||I||" (USAGE)");
        ATMLAG=COMPRESS("ATMLAG"||I||"=LAG"||I||" (ATM)");
        LAG="IF "||COMPRESS("ATMLAG"||I)||"=ATM THEN "
            ||COMPRESS("LAG"||I||"=TMP_LAG"||I||");";
        OUTPUT;
    END;
RUN;

```

	TMP_LAG	ATMLAG	LAG
1	TMP_LAG1=LAG1(USAGE);	ATMLAG1=LAG1(ATM);	IF ATMLAG1=ATM THEN LAG1=TMP_LAG1;
2	TMP_LAG2=LAG2(USAGE);	ATMLAG2=LAG2(ATM);	IF ATMLAG2=ATM THEN LAG2=TMP_LAG2;
3	TMP_LAG3=LAG3(USAGE);	ATMLAG3=LAG3(ATM);	IF ATMLAG3=ATM THEN LAG3=TMP_LAG3;
4	TMP_LAG4=LAG4(USAGE);	ATMLAG4=LAG4(ATM);	IF ATMLAG4=ATM THEN LAG4=TMP_LAG4;

Figure 2. Tmp table to extract global variable reference

```

*STEP 2) CREATE GLOBAL VARIABLES;
PROC SQL NOPRINT;
  SELECT TMP_LAG INTO:TMP_LAG SEPARATED BY ' ' FROM TMP ;
  SELECT ATMLAG INTO:ATMLAG SEPARATED BY ' ' FROM TMP ;
  SELECT LAG INTO:LAG SEPARATED BY ' ' FROM TMP ;
QUIT;

*STEP 3) INSERTING THE MACRO VARIABLES IN ORDER TO EXECUTE THE N-LAG FUNCTIONS;
DATA IMPUTED_LAG_NO_ET;
  SET IMPUTED;
  BY ATM;
  &TMP_LAG.
  &ATMLAG.
  &LAG.
  ;
  DROP TMP_LAG1--ATMLAG&LAGS.;
RUN;

```

	atm	trandate	usage	LAG1	LAG2	LAG3	LAG4	LAG5	LAG6	LAG
730	NN5_001	17MAR1998	32.341269841	19.699546485	24.985827664	37.159863946	47.16553288	60.161564626	38.633786848	30.661
731	NN5_001	18MAR1998	30.087868481	32.341269841	19.699546485	24.985827664	37.159863946	47.16553288	60.161564626	38.633
732	NN5_001	19MAR1998	54.138321995	30.087868481	32.341269841	19.699546485	24.985827664	37.159863946	47.16553288	60.161
733	NN5_001	20MAR1998	53.500566893	54.138321995	30.087868481	32.341269841	19.699546485	24.985827664	37.159863946	47.161
734	NN5_001	21MAR1998	39.696712018	53.500566893	54.138321995	30.087868481	32.341269841	19.699546485	24.985827664	37.159
735	NN5_001	22MAR1998	29.70521542	39.696712018	53.500566893	54.138321995	30.087868481	32.341269841	19.699546485	24.985
736	NN5_002	18MAR1996	11.550453515
737	NN5_002	19MAR1996	13.591269841	11.550453515
738	NN5_002	20MAR1996	15.036848073	13.591269841	11.550453515
739	NN5_002	21MAR1996	21.570294785	15.036848073	13.591269841	11.550453515
740	NN5_002	22MAR1996	27.253401361	21.570294785	15.036848073	13.591269841	11.550453515	.	.	.
741	NN5_002	23MAR1996	11.706349206	27.253401361	21.570294785	15.036848073	13.591269841	11.550453515	.	.
742	NN5_002	24MAR1996	14.937641723	11.706349206	27.253401361	21.570294785	15.036848073	13.591269841	11.550453515	.
743	NN5_002	25MAR1996	12.244897959	14.937641723	11.706349206	27.253401361	21.570294785	15.036848073	13.591269841	11.550
744	NN5_002	26MAR1996	15.504535147	12.244897959	14.937641723	11.706349206	27.253401361	21.570294785	15.036848073	13.591
745	NN5_002	27MAR1996	18.934240363	15.504535147	12.244897959	14.937641723	11.706349206	27.253401361	21.570294785	15.036

Figure 3. Imputed_lag_no_ets table results

Filling in for missing lags- SAS/ETS solution

An obvious consequence of adding a large degree of lag variables into any time series model is the increasing number of missing values. As seen in the screen shot in the previous page, when the number of lags increases so does the number of missing values at the beginning of the time series. This renders an increasing number of observations that will be thrown out in the model if these missing values are not imputed. This is one of the major advantages of utilizing proc panel as there are 4 different methods of instantly imputing these missing values when producing the lag columns. Replacing the Lag statement with any of the 4 following statements will cause the missing values to be imputed by the chosen method:

CLAG, SLAG, XLAG, ZLAG.

CLAG: replaces missing values with the cross section mean for that variable in that cross section. For example if an ATM had a missing value for of lag4 for 23Mar1996 then those values are filled in with the overall average for that ATM.

SLAG: replaces missing values with the average corresponding lag of other entities. For example if an ATM had a missing value for lag4 for 23Mar1996 and there were 2 other ATMS that had lag4 volumes for the 23Mar1996 the missing value of the first ATM would be replaced with the average of lag4 for the 2 other ATMs.

XLAG: replaces missing values with average of all volumes. For example if an ATM had a missing value for lag4 for 23Mar1996 then the missing values would be replaced by the average of all volumes of all days and ATMs

ZLAG: replaces missing values 0

CLAG/SLAG/XLAG/ZLAG demonstrations:

Consider a data set of 3 ATM –NN5_001, NN5_002, NN5_003 with only one missing value for ATM NN5_001 on Mar24, 1996.

	atm	trandate	usage
1	NN5_001	18MAR1996	13.407029478
2	NN5_001	19MAR1996	14.725056689
3	NN5_001	20MAR1996	20.564058957
4	NN5_001	21MAR1996	34.708049887
5	NN5_001	22MAR1996	26.629818594
6	NN5_001	23MAR1996	16.609977324
7	NN5_001	24MAR1996	.
8	NN5_001	25MAR1996	11.607142857
9	NN5_001	26MAR1996	19.883786848
10	NN5_001	27MAR1996	23.767006803

Figure 4. Train table for demonstrating proc panel results

CLAG: fills in all missing values filled with 28.643468- This is the average of all usage of ATM “NN5_001”.

```
PROC PANEL DATA=TRAIN;
  ID ATM TRANDATE;
  CLAG USAGE (0 1 2 3) /OUT=CLAG;
RUN;
```

	atm	trandate	usage	usage_0	usage_1	usage_2	usage_3
1	NN5_001	18MAR1996	13.407029	13.407029	28.643468	28.643468	28.643468
2	NN5_001	19MAR1996	14.725057	14.725057	13.407029	28.643468	28.643468
3	NN5_001	20MAR1996	20.564059	20.564059	14.725057	13.407029	28.643468
4	NN5_001	21MAR1996	34.70805	34.70805	20.564059	14.725057	13.407029
5	NN5_001	22MAR1996	26.629819	26.629819	34.70805	20.564059	14.725056
6	NN5_001	23MAR1996	16.609977	16.609977	26.629819	34.70805	20.564058
7	NN5_001	24MAR1996	.	28.643468	16.609977	26.629819	34.708049
8	NN5_001	25MAR1996	11.607143	11.607143	28.643468	16.609977	26.629818
9	NN5_001	26MAR1996	19.883787	19.883787	11.607143	28.643468	16.609973
10	NN5_001	27MAR1996	23.767007	23.767007	19.883787	11.607143	28.643468
11	NN5_001	28MAR1996	34.027778	34.027778	23.767007	19.883787	11.607142
12	NN5_001	29MAR1996	33.786848	33.786848	34.027778	23.767007	19.883786
13	NN5_001	30MAR1996	18.253968	18.253968	33.786848	34.027778	23.767006
14	NN5_001	31MAR1996	19.387755	19.387755	18.253968	33.786848	34.027777

Figure 5. Clag table-Results using Clag option

SLAG: fills in the missing values for the according date of Mar 24, 1996 with the average for the usage in ATMs NN5_002 and NN5_003 of 13.236961451. However as the future lags are calculated rather than carrying this value down the average of the respective Lag is the fill in value for that lag. For example lag1 the average of the usage on May 25, 1997 of ATMs NN5_002 and NN5_003 is 11.531557067 which is not the normal carry down of 13.236961451. Also notice that the average for the backfill dates is the average of all 3 ATM

```

PROC PANEL DATA=TRAIN;
  ID ATM TRANDATE;
  SLAG USAGE(0 1 2 3) /OUT=SLAG;
RUN;

```

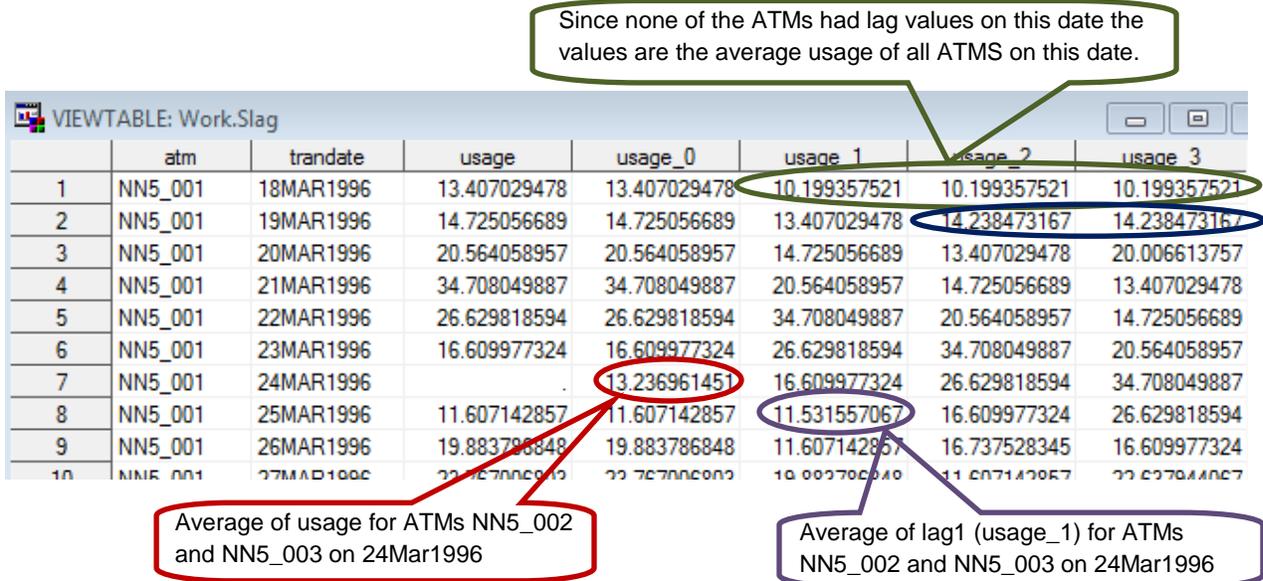


Figure 6. Slag table-Results using Slag option

XLAG: fills in all missing values with the overall average of all volumes. The Average for the 3 atms over all dates is 22.683851974.

```

PROC PANEL DATA=TRAIN;
  ID ATM TRANDATE;
  XLAG USAGE(0 1 2 3) /OUT=XLAG;
RUN;

```

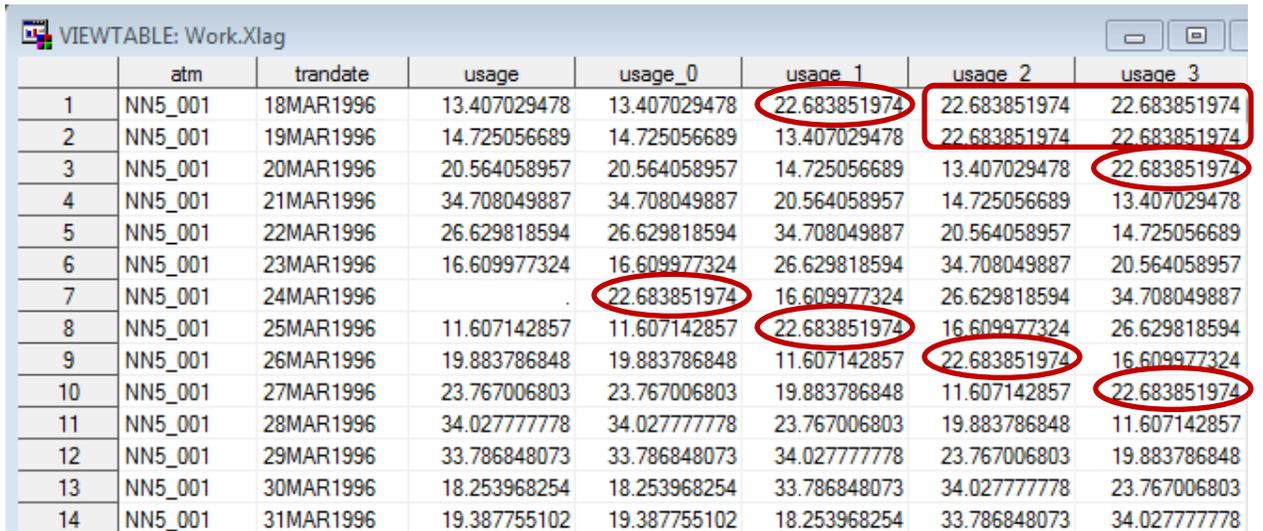


Figure 7. Xlag table-Results using Xlag option

ZLAG Fills in all missing Values with 0.

```

PROC PANEL DATA=TRAINTMP;
  ID ATM TRANDATE;
  ZLAG USAGE(0 1 2 3) /OUT=ZLAG;
RUN;

```

VIEWTABLE: Work.Zlag							
	atm	trandate	usage	usage_0	usage_1	usage_2	usage_3
1	NN5_001	18MAR1996	13.407029478	13.407029478	0	0	0
2	NN5_001	19MAR1996	14.725056689	14.725056689	13.407029478	0	0
3	NN5_001	20MAR1996	20.564058957	20.564058957	14.725056689	13.407029478	0
4	NN5_001	21MAR1996	34.708049887	34.708049887	20.564058957	14.725056689	13.407029478
5	NN5_001	22MAR1996	26.629818594	26.629818594	34.708049887	20.564058957	14.725056689
6	NN5_001	23MAR1996	16.609977324	16.609977324	26.629818594	34.708049887	20.564058957
7	NN5_001	24MAR1996	.	0	16.609977324	26.629818594	34.708049887
8	NN5_001	25MAR1996	11.607142857	11.607142857	0	16.609977324	26.629818594
9	NN5_001	26MAR1996	19.883786848	19.883786848	11.607142857	0	16.609977324
10	NN5_001	27MAR1996	23.767006803	23.767006803	19.883786848	11.607142857	0
11	NN5_001	28MAR1996	34.027777778	34.027777778	23.767006803	19.883786848	11.607142857
12	NN5_001	29MAR1996	33.786848073	33.786848073	34.027777778	23.767006803	19.883786848
13	NN5_001	30MAR1996	18.253968254	18.253968254	33.786848073	34.027777778	23.767006803
14	NN5_001	31MAR1996	19.387755102	19.387755102	18.253968254	33.786848073	34.027777778

Figure 8. Zlag table-Results using Zlag option

Filling in for missing lags- non-SAS/ETS solution

There are of course and infinite number of ways to deal with these missing values. The proposed method is to take the assumed most known significant cycle and use that number of forward lags to back fill. In the case of ATM Volumes Weekday volumes tend to be the most significant signal for ATMS. For this reason lag 7 is calculated for the reverse order of the ATM and then used to fill in for any missing values.

The steps to carry out this weekday closest lag solution are:

- 1) Sort the data by atm, weekday and descending trandate
- 2) Create a series of n-temporary variables to be referenced as a single global variable
- 3) Using array and retain statements reset each n-temporary variable to missing if either the first atm or first weekday. Using a do loop with the arrays to assign each lag variable to the last corresponding lag value.

VIEWTABLE: Work.Imputing_needed									
	atm	trandate	usage	LAG1	LAG2	LAG3	LAG4	LAG5	LAG6
1	NN5_001	18MAR1996	13.407029478
2	NN5_001	19MAR1996	14.725056689	13.407029478
3	NN5_001	20MAR1996	20.564058957	14.725056689	13.407029478
4	NN5_001	21MAR1996	34.708049887	20.564058957	14.725056689	13.407029478	.	.	.
5	NN5_001	22MAR1996	26.629818594	34.708049887	20.564058957	14.725056689	13.407029478	.	.
6	NN5_001	23MAR1996	16.609977324	26.629818594	34.708049887	20.564058957	14.725056689	13.407029478	.
7	NN5_001	24MAR1996	15.320294785	16.609977324	26.629818594	34.708049887	20.564058957	14.725056689	13.407029478
8	NN5_001	25MAR1996	11.607142857	15.320294785	16.609977324	26.629818594	34.708049887	20.564058957	14.725056689
9	NN5_001	26MAR1996	19.883786848	11.607142857	15.320294785	16.609977324	26.629818594	34.708049887	20.564058957
10	NN5_001	27MAR1996	23.767006803	19.883786848	11.607142857	15.320294785	16.609977324	26.629818594	34.708049887
11	NN5_001	28MAR1996	34.027777778	23.767006803	19.883786848	11.607142857	15.320294785	16.609977324	26.629818594
12	NN5_001	29MAR1996	33.786848073	34.027777778	23.767006803	19.883786848	11.607142857	15.320294785	16.609977324
13	NN5_001	30MAR1996	18.253968254	33.786848073	34.027777778	23.767006803	19.883786848	11.607142857	15.320294785

Figure 9. Imputing_needed table-demonstrating which values need to be shifted up

```

Step 1) *ADDING WEEKDAY IN ORDER TO SORT BY WEEKDAY;
DATA IMPUTING_NEEDED;
    SET LAG360_NO_ETC;
    WKDY=WEEKDAY (TRANDATE) ;
RUN;

PROC SORT DATA= IMPUTING_NEEDED;
    BY ATM WKDY DESCENDING TRANDATE;
RUN;

```

Step 2) *CREATING A LIST OF N# OF TEMPORARY VARIABLES FOR RETAIN STATEMENT;

```

DATA TMP;
    FORMAT TMP $8.;
    DO I=1 TO &LAGS.;
        TMP="T"||LEFT(I);
        OUTPUT;
    END;
RUN;
PROC SQL NOPRINT;
    SELECT TMP INTO:TMP SEPARATED BY ' ' FROM TMP ;
QUIT;

```

Step 3) *USING THE RETAIN AND ARRAY STATEMENTS TO FILL IN MISSING VALUES WITH CLOSEST WEEKDAY LAG VALUE;

```

DATA IMPUTED(DROP=WKDY);
    SET IMPUTING_NEEDED;
    BY ATM WKDY;
    RETAIN &TMP.;
    ARRAY L{*} LAG1--LAG&LAGS.;
    ARRAY T{*} T1--T&LAGS.;
*ENSURING VALUE OF OTHER ATMS OR WEEKDAYS DO NOT CROSS OVER;
    IF FIRST.ATM OR FIRST.WKDY THEN DO I=1 TO &LAGS.;
        T(I)=.;
    END;
    DO I=1 TO &LAGS.;
*ONLY REPLACES LAG VARIABLE IF MISSING WITH LATEST NON MISSING WEEKDAY VOLUME;
        IF L(I)=. THEN L(I)=T(I);
*SET TEMPORARY LAG-N VARIABLES TO LATESTEST LAG-N VALUE;
        T(I)=L(I);
    END;
DROP I &TMP.;
RUN;

PROC SORT DATA=IMPUTED;
    BY ATM TRANDATE;
RUN;

```

	atm	trandate	usage	LAG1	LAG2	LAG3	LAG4	LAG5	LAG6
1	NN5_001	18MAR1996	13.407029478	15.320294785	16.609977324	26.629818594	34.708049887	20.564058957	14.725056689
2	NN5_001	19MAR1996	14.725056689	13.407029478	15.320294785	16.609977324	26.629818594	34.708049887	20.564058957
3	NN5_001	20MAR1996	20.564058957	14.725056689	13.407029478	15.320294785	16.609977324	26.629818594	34.708049887
4	NN5_001	21MAR1996	34.708049887	20.564058957	14.725056689	13.407029478	15.320294785	16.609977324	26.629818594
5	NN5_001	22MAR1996	26.629818594	34.708049887	20.564058957	14.725056689	13.407029478	15.320294785	16.609977324
6	NN5_001	23MAR1996	16.609977324	26.629818594	34.708049887	20.564058957	14.725056689	13.407029478	15.320294785
7	NN5_001	24MAR1996	15.320294785	16.609977324	26.629818594	34.708049887	20.564058957	14.725056689	13.407029478
8	NN5_001	25MAR1996	11.607142857	15.320294785	16.609977324	26.629818594	34.708049887	20.564058957	14.725056689
9	NN5_001	26MAR1996	19.883786848	11.607142857	15.320294785	16.609977324	26.629818594	34.708049887	20.564058957
10	NN5_001	27MAR1996	23.767006803	19.883786848	11.607142857	15.320294785	16.609977324	26.629818594	34.708049887
11	NN5_001	28MAR1996	34.027777778	23.767006803	19.883786848	11.607142857	15.320294785	16.609977324	26.629818594
12	NN5_001	29MAR1996	33.786848073	34.027777778	23.767006803	19.883786848	11.607142857	15.320294785	16.609977324
13	NN5_001	30MAR1996	18.253968254	33.786848073	34.027777778	23.767006803	19.883786848	11.607142857	15.320294785
14	NN5_001	31MAR1996	19.387755102	18.253968254	33.786848073	34.027777778	23.767006803	19.883786848	11.607142857

Figure 10. Imputed table results of shifting values up

CONCLUSION

Creating iterative variables using the proposed 3 step method to invoking command syntax stored as macro variables can save on coding time and is more robust to non detectable log type errors. This process is particular useful in that it can be applied to any other similar scenario as the demonstrated multiple lagged scenario in order to implement

REFERENCES

- Source data used to demonstrate techniques originated from the NN5 Competition and was “pre-imputed” to fill in for missing dates/values prior to the execution of all techniques demonstrated. The source data of NN5 may be found at: <http://www.neural-forecasting-competition.com/downloads/NN5/datasets/download.htm>

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RECOMMENDED READING

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